

**Concept Question 2-1:** What three properties must an LTI system have?

The **scaling property**, which states that if the response to input  $x(t)$  is output  $y(t)$ , then the response to input  $cx(t)$  is output  $cy(t)$  for any constant  $c$ .

The **additivity property**, which states that if the response to input  $x_1(t)$  is output  $y_1(t)$ , and the response to input  $x_2(t)$  is output  $y_2(t)$ , then the response to input  $(x_1(t) + x_2(t))$  is output  $(y_1(t) + y_2(t))$ .

The additivity and scaling properties together are called the **superposition property**. A system with these two properties is linear.

The third property of a LTI system is **time invariance**, which states that if the response to input  $x(t)$  is output  $y(t)$ , then the response to input  $x(t - T)$  is output  $y(t - T)$  for any constant  $T$ . A linear system that is also time-invariant is linear time-invariant (LTI).