

**Concept Question 3-10:** Why is a system with an improper transfer function always BIBO unstable?

The partial fraction expansion of an improper  $\mathbf{H}(s)$  includes a term proportional to  $s$ . See Eq. (3.104) for an example. Consider a bounded input  $x(t) = u(t)$ . Then  $\mathbf{X}(s) = 1/s$  and  $\mathbf{Y}(s) = \mathbf{H}(s) \mathbf{X}(s)$  includes a constant term, whose inverse Laplace transform is an impulse, so the output is unbounded.