Concept Question 7-23: Why is the FFT so much faster than direct computation of the DFT?

Because direct computation of the N-point DFT of a signal of duration N requires about N^2 computations, while the same computation using the FFT requires only about $(N/2) \log_2 N$ computations.